



# QCD, NUCLEAR PDF and

# CUMULATIVE PROCESSES

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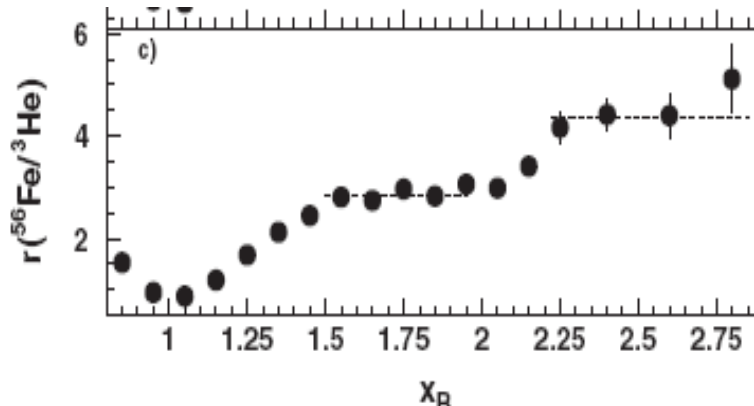
A.Efremov, JINR, Dubna, [PLB174(86)319 and hep-ph/9710477]

## Content

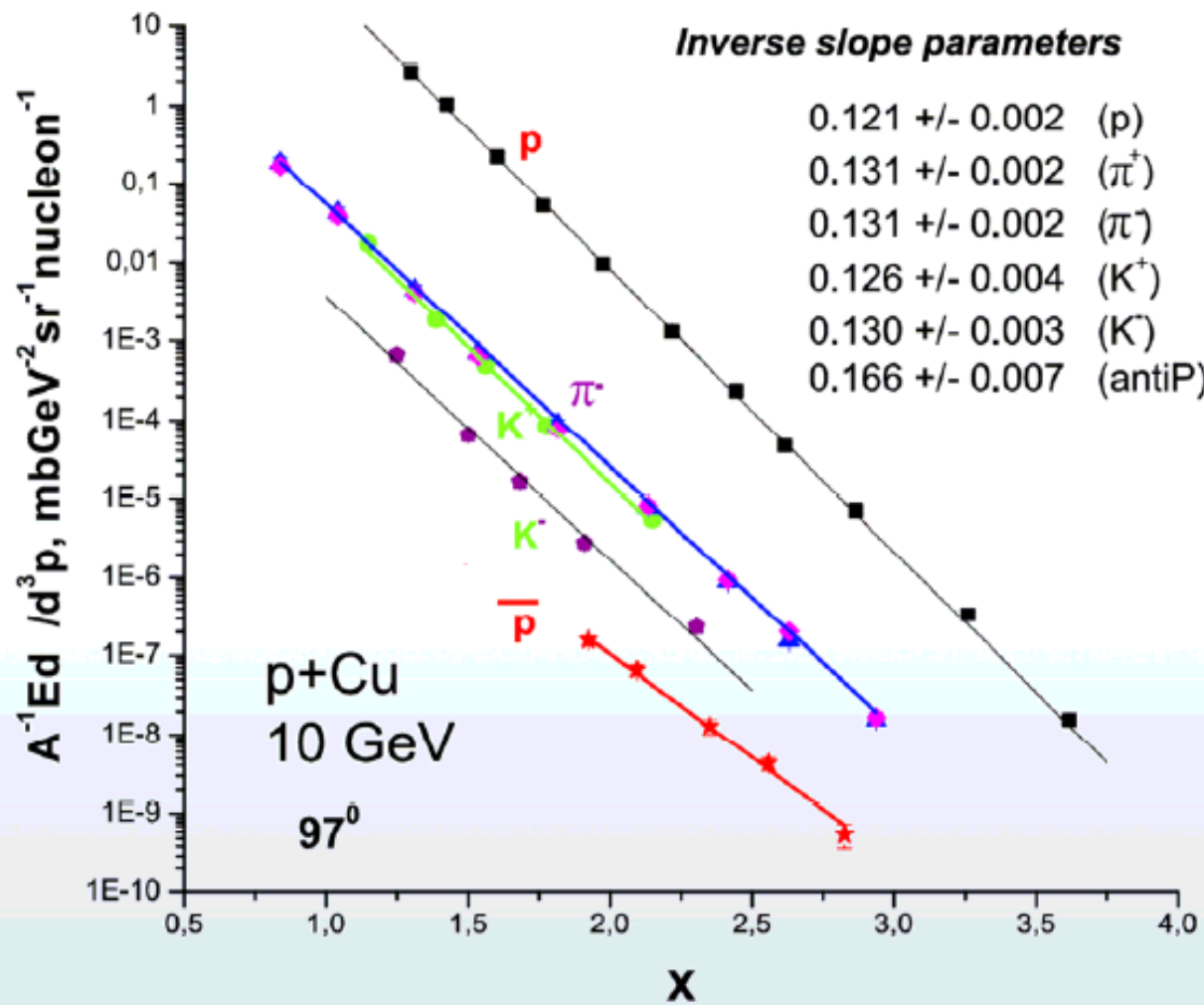
- 1. Nucleon and Nuclear PDF's
- 2. The EMC Effect
- 3. Cumulative Particle Production
- 4. Sea Particles and Multiquarks
- 5. Conclusions

# Some short history

- 1957-- Leksin G.A. at al. -- Intensive backward protons discovery
- 1957 -- Mescheryakov M.G. – Intensive knock out of deuterons from nuclei
- 1957 -- Blokhintsev D.I. – Hypothesis about “fluctons”.
- 1971 -- Baldin, Stavinski at al. – Proposal and discovery of cumulative pions  
 $D(5 \text{ GeV}/N) + Cu \rightarrow \pi(7 \text{ GeV}) + X$
- Mid of 70's -- Dubna, ITEP, Erevan -- Intensive experimental studies of cumulative particle production
- 1976 – AE – Nuclear quark-gluon structure
- 1976 – Frankfurt, Strikman – Short range FNC  
 “Could” and “Hot” models
- 1983 – EMC collaboration – brings important news -- EMC1-effect
- 1984 – Savin (BCDMS) –  $F_2^A(x)$  beyond  $x>1$ , in favor of “Could” models
- 2006 – Egiyan et al. (CLAS e-A→e-X) -- clear step behavior of the ratio



$$R(A, ^3\text{He}) = \frac{3\sigma_A(Q^2, x_B)}{A\sigma_{^3\text{He}}(Q^2, x_B)}$$

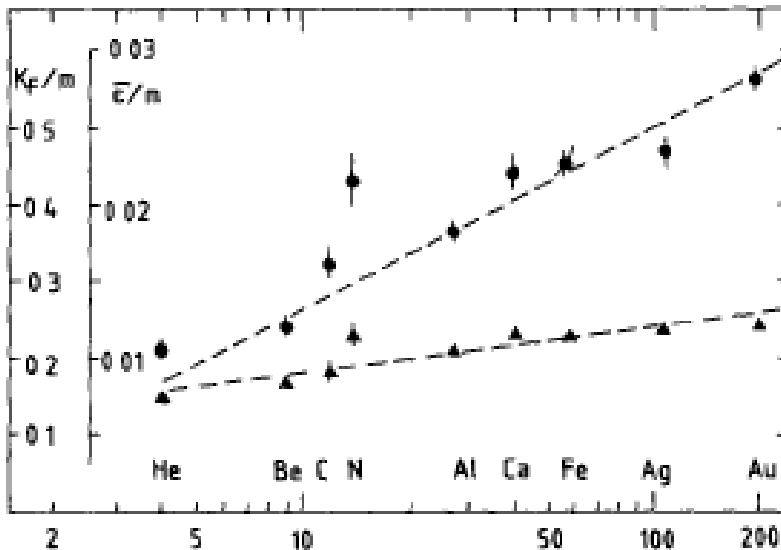
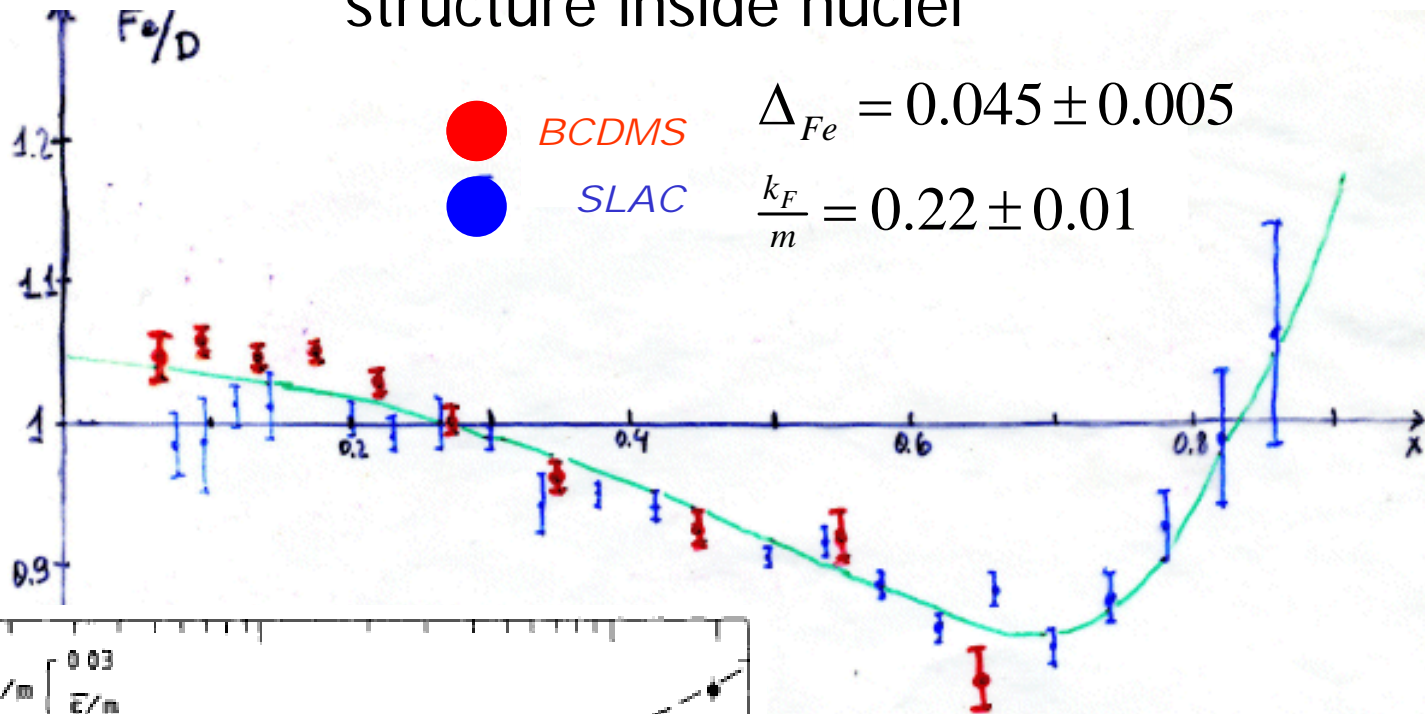


FAS @ ITEP  
(Boyarinov et.al  
Yad.Fiz 57  
(1994) 1452)

X – minimal target mass [ $m_N$ ] needed to produce particle

# New information from

## Nuclear EMC-effect – change of nucleon structure inside nuclei



The  $A$ -dependence of the parameters  $\epsilon/m$  (●) and  $k_F/m$  (▲) obtained from SLAC and NA4 ( $A = 14, 56$ ) data.

# 1. Nucleon and Nuclear PDF's

QCD evolution equations **do not depend on kind of object.**

$$\frac{\dot{V}_A(n, Q^2)}{V_A(n, Q^2)} = \frac{\dot{V}_N(n, Q^2)}{V_N(n, Q^2)} = \gamma_N(\alpha_S(Q^2)) \cdot \equiv \frac{d}{d \log Q^2}$$

*n* - moment number

or

$$V_A(n, Q^2) = T_A^{NS}(n) V_N(n, Q^2) \quad (1)$$

or

$$xF_{3A} \approx V_A(x, Q^2) = \int_x^A d\alpha T_A^{NS}(\alpha) V_N\left(\frac{x}{\alpha}, Q^2\right) \quad (2)$$

with baryon number sum rule: (All nuclear function here are normalized to A.)

$$\int_0^A d\alpha T_A^{NS}(\alpha) = 1$$

**Singlet channel** (Assume no "primordial" gluon distribution, i.e. all gluons results in QCD evolution.)

$$\Sigma_A(x, Q^2) = \int_x^A d\alpha T_A^S(\alpha) \Sigma_N\left(\frac{x}{\alpha}, Q^2\right) \quad (3)$$

$$G_A(x, Q^2) = \int_x^A d\alpha T_A^S(\alpha) G_N\left(\frac{x}{\alpha}, Q^2\right) \quad (4)$$

In general,  $T^S \neq T^{NS}$  and  $T^S$  satisfies energy-momentum sum rule

$$\int_0^A d\alpha \alpha T_A^S(\alpha) = \frac{M_A}{AM_N} \approx 1 \quad (5)$$

Immediate consequence of Eqs. (3,4)  $\frac{\langle x_G \rangle_A}{\langle x_G \rangle_N} = \frac{\langle x_q \rangle_A}{\langle x_q \rangle_N} = 1$

**Clearly contradict rescaling hypothesis!**

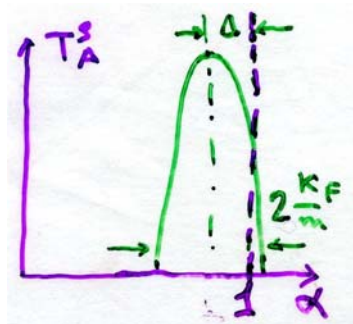
**Notice:** QCD evolution is **leading twist approximation**. **Nuclear screening** (formally, a high twist effect) **is not included**.

Levin,Ryskin(85),  
Brodsky,Hoyer(91,92)  
Indumathi(96)

## 2. The EMC Effect

$T_A$  is, approximately, an effective distribution of nucleons in nucleus. Concentrated at  $\alpha = 1$  (zero internal momentum).

Expanding (1) and (3) around  $\alpha = 1$  one have:



$\langle \dots \rangle$  means integration over interval  $0 < \alpha < A$ .

$$R = \frac{F_A}{F_N} \simeq \langle T \rangle + \langle (1 - \alpha)T \rangle x \frac{F'_N}{F_N} \quad (7)$$

$$+ \frac{1}{2} \langle (1 - \alpha)^2 T \rangle x \left[ x \frac{F''_N}{F_N} + 2 \frac{F'_N}{F_N} \right] + \dots$$

$= -3x/(1-x)$

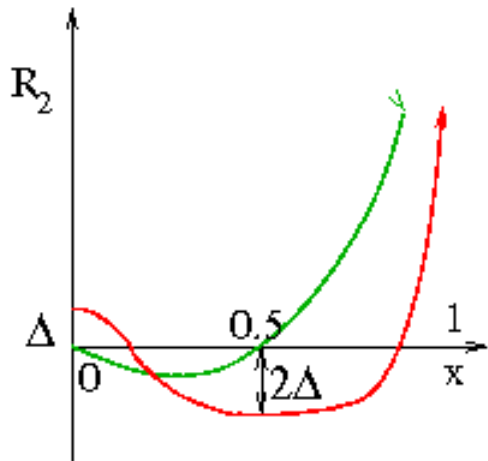
$= 0$  at  $x=0.5$  and  $F \sim (1-x)^3$

For ratio of  $F_2 \approx \Sigma$

$$\langle T_A^S \rangle - 1 = \Delta_A > 0 \quad \text{or}$$

$$\int_0^A d\alpha [T_A^S(\alpha) - T_A^{NS}(\alpha)] = \Delta_A > 0 \quad (8)$$

$$\int_0^A d\alpha \alpha [T_A^S(\alpha) - T_A^{NS}(\alpha)] = \delta_A > 0 \quad (9)$$



Since  $R_3 \approx R_2$  near  $x \approx 0.5$  (no sea quarks)  $\delta_A \approx \frac{2}{3} \Delta_A$

## Conclusions on EMC:

- Effective nucleons" number larger than  $A$ ,
- Valence nucleons carry only a part of total nucleus momentum,
- EMC-effect is result of repumping a part of momentum from valence quarks to sea quarks.

### • Immediate consequences:

$$i. R_2(x \simeq 0) = \frac{A}{f} \int_0^1 d\alpha T_A^S(\alpha) = 1 + \Delta_A > 1$$

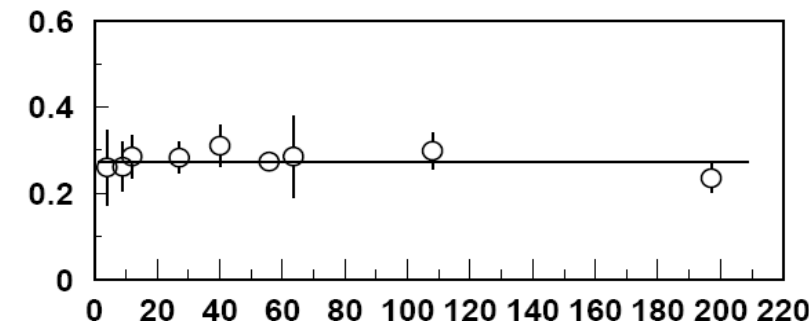
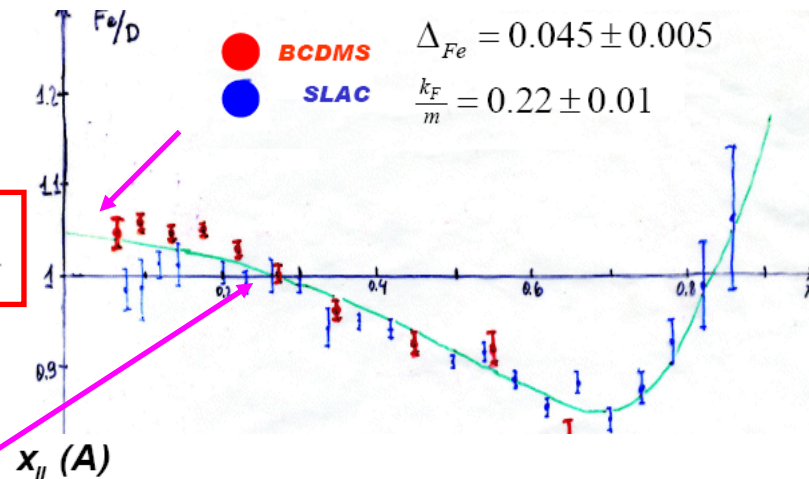
Seen by BCDMS,  $\Delta_{Fe} = 0.045 \pm 0.005$

(Recall: screening phenomena are disregarded!)

$$ii. R_2(x \simeq 0.3) = 1 \text{ independent on } A.$$

Seen by SLAC, BCDMS, EMC.

G.Smirnov, *Phys.Atom.Nucl.* **58** (1995) 1613





iii. Small ( $\approx \Delta_A$ ) but **hard "collective" sea**

$$O_A(x, Q^2) \equiv \Sigma_A - V_A = \int_x^A d\alpha T_A^{NS}(\alpha) O_N\left(\frac{x}{\alpha}, Q^2\right) +$$

**Internucleon sea**

$$+ \int_x^A d\alpha [T_A^S(\alpha) - T_A^{NS}(\alpha)] \Sigma_N\left(\frac{x}{\alpha}, Q^2\right) \quad (11)$$

**Collective nuclear sea  $O'_A$**

$$\bar{\alpha}_{O'} = \frac{\langle \alpha (T_A^S - T_A^{NS}) \rangle}{\langle T_A^S - T_A^{NS} \rangle} = \frac{\delta_A}{\Delta_A} \approx 1 (=2/3)$$

Can be seen in excess of hard "sea" particles ( $K, \bar{P}, J/\psi$ )

**Models:** Different ways of repumping: *Llewellyn-Smith(83), Ericson, Thomas(83)*

- a. Repumping to a heavy components ( $\rho, \omega, \bar{N}N$ -pairs, off-shell  $\pi$ ),
- b. Repumping inside each nucleon, *Frankfurt, Strikman(82), Barone et.al., Szwed(83)*
- c. Repumping inside multiquarks.  $\Delta_A \approx \rho_A \Delta_{6q} + \dots \ll \Delta_{6q}$  *Lot of authors*

# 3. Cumulative Particle Production

Common property quark-parton models for inclusive production:

$$\frac{\epsilon}{A} \frac{d\sigma}{d^3p} = \rho_{A \rightarrow h}(x, y, p_T) = \int \frac{A d\alpha}{x \alpha} F_A(\alpha) f_h\left(\frac{x}{\alpha}, y, p_T\right) \quad (12)$$

$(x=u/s, y=-t/s)$   $f_h$  is model dependent but does not depend on A.

## Models:

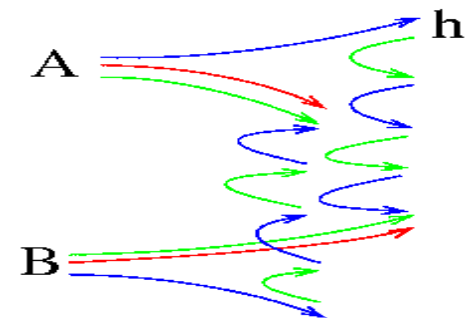
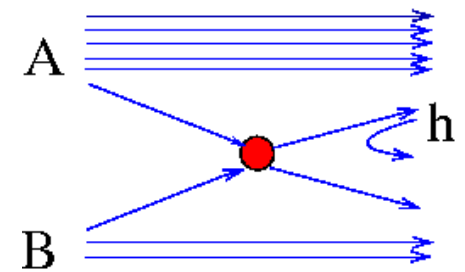
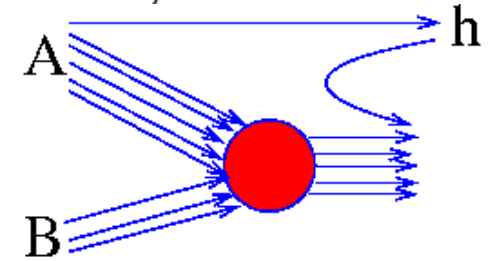
- Limiting fragmentation. Coaliscent:

$$r_A \sim F_A, f(x/\alpha) \sim \delta(x/\alpha - 1)$$

- Hard scattering:  $f\left(\frac{x}{\alpha}\right) = \int_{\frac{y}{1-x/\alpha}}^1 d\beta F_B(\beta) D_h\left(\frac{x}{\alpha} + \frac{y}{\beta}\right) \frac{d\sigma}{dt}\left(p_T, \frac{x}{\alpha}, \frac{y}{\beta}\right)$

- Dual string:  $f\left(\frac{x}{\alpha}\right) = D_h\left(\frac{x}{\alpha} + \frac{y}{\beta}\right)$

Combining (12) with (1,3) one has:



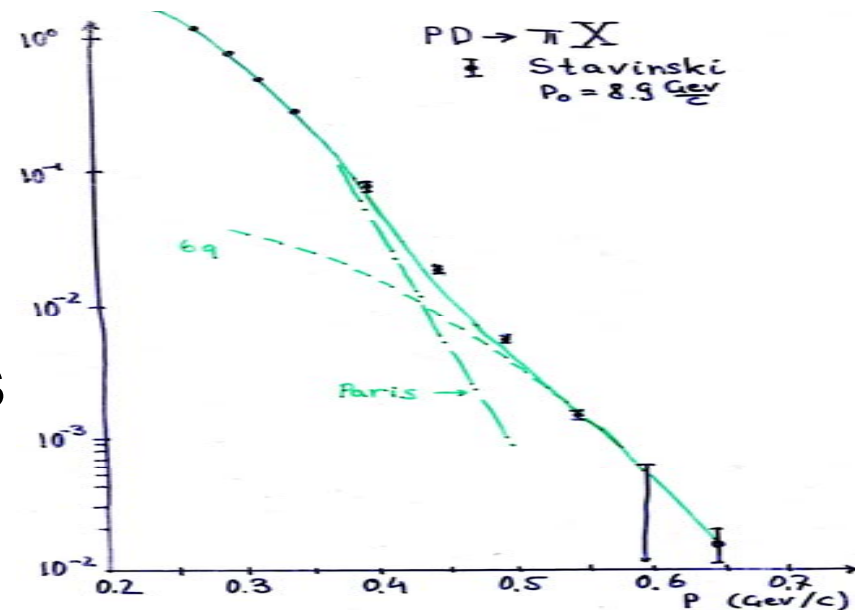
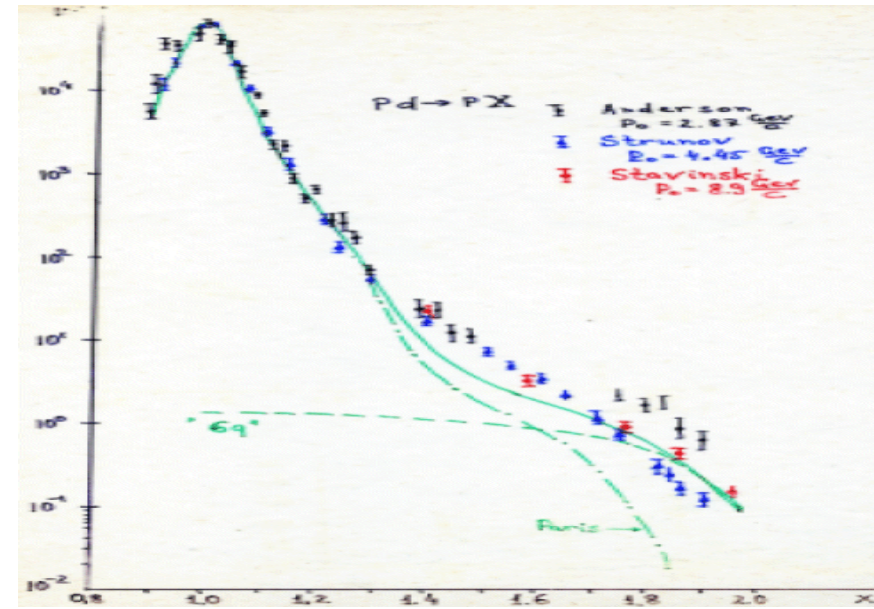
$$\rho_{A \rightarrow h}(x, y, p_T) = \int_x^A d\alpha N_A(\alpha) \rho_{N \rightarrow h}\left(\frac{x}{\alpha}, y, p_T\right) + \int_x^A d\alpha \tilde{N}_A(\alpha) \rho_{\tilde{N} \rightarrow h}\left(\frac{x}{\alpha}, y, p_T\right) \quad (13)$$

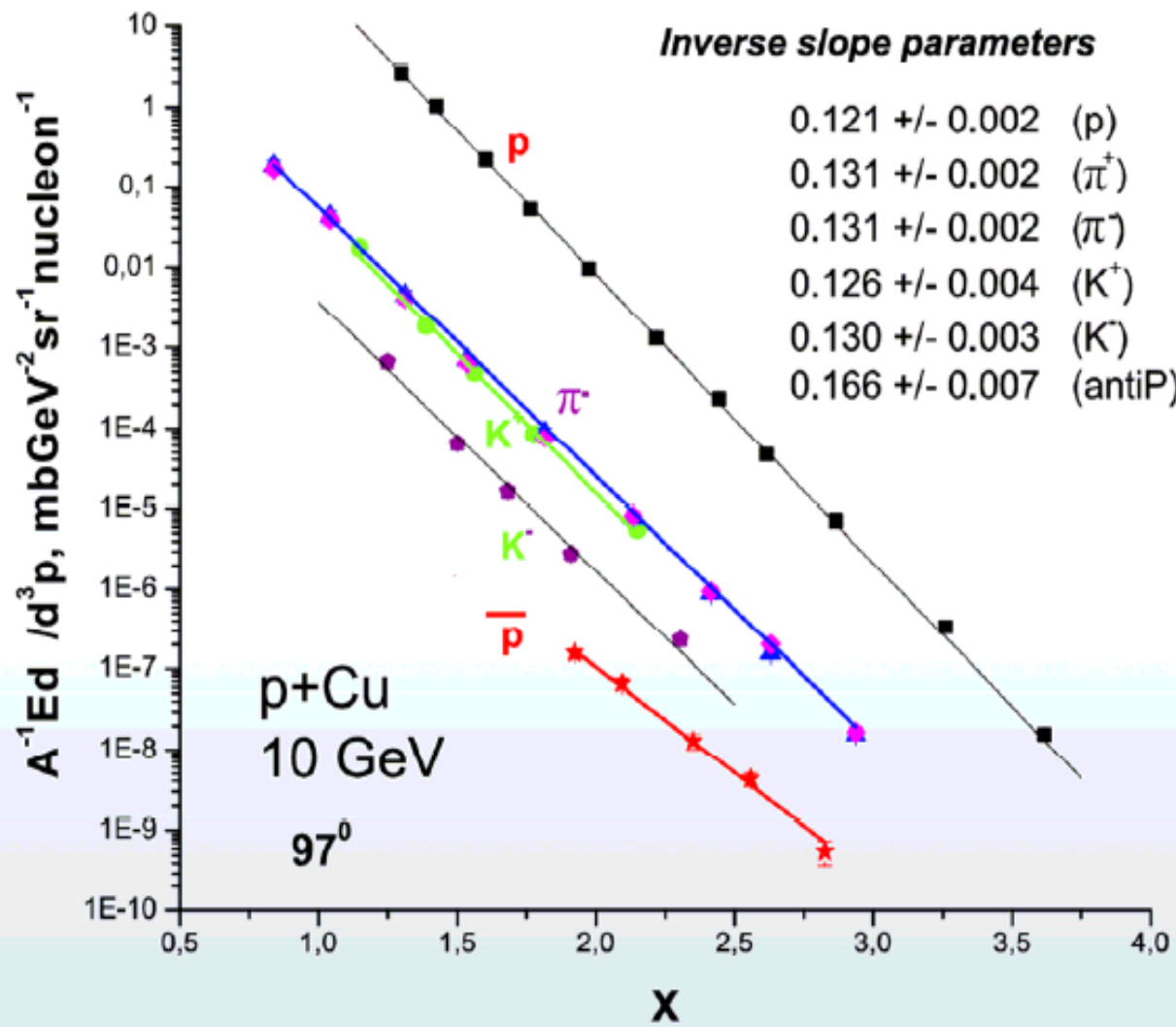
$$N_A = \frac{1}{2} (T_A^S + T_A^{NS}) \quad \text{and} \quad \tilde{N}_A = \frac{1}{2} (T_A^S - T_A^{NS})$$

$N_A$  can be found from stripped **cumulative proton** spectrum with  $p_T = 0$ .

(AE, Kajdalov, et.al. YaF(88,99))

Cumulative  $\pi$  and  $K^+$  than determines by (13) with experimental  $\rho_{N \rightarrow \pi}$  **with no new parameters!** ( $\tilde{N}_A$  term is small).





FAS @ ITEP  
(Boyarinov et.al  
Yad.Fiz 57  
(1994) 1452)

X – minimal target mass [  $m_N$  ] needed to produce particle

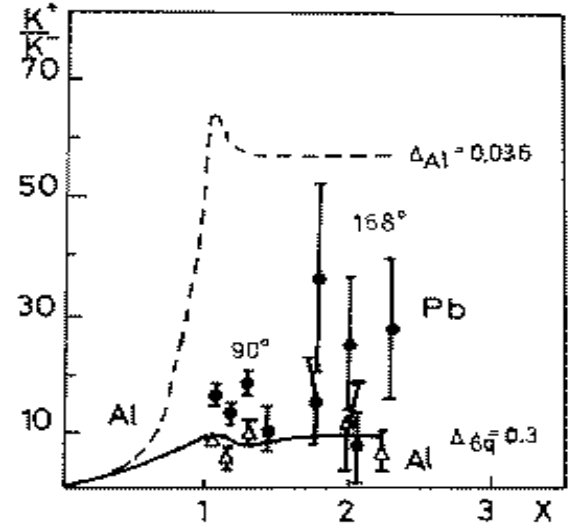
# 4. Sea Particles and Multiquarks

The most intriguing. Discriminates "6q" and FNC.

$$r_A = \frac{K^+}{K^-} \approx \frac{\int \frac{d\alpha}{x} N_A(\alpha) \rho_{N \rightarrow K^+}(\frac{x}{\alpha})}{\int \frac{d\alpha}{x} \bar{N}_A(\alpha) \rho_{N \rightarrow K^+}(\frac{x}{\alpha})} \approx \frac{2}{\Delta} 6q$$

(approximation  $\rho_{\bar{N} \rightarrow K^-} \approx \rho_{N \rightarrow K^+}$  was used.)

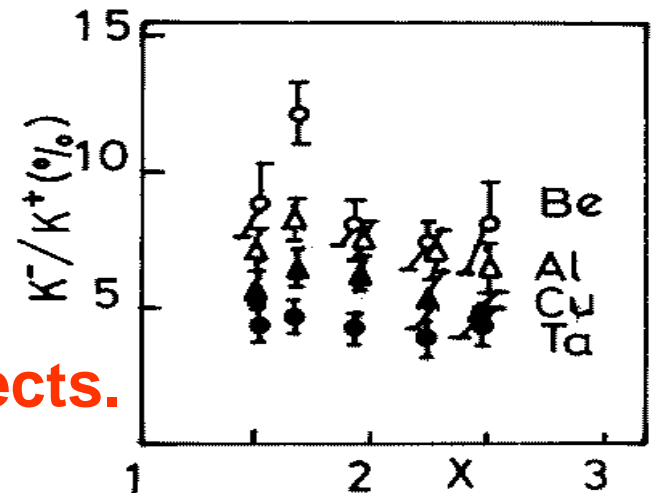
**Experiment:**  $r_A$  const(x) for  $1 < x < 2.5$  and surprisingly small compared with expected from EMC-effect



(Baldin at al. (82),  $E_{lab}=8,9$  GeV,  $\theta_{lab}=168^\circ$ )

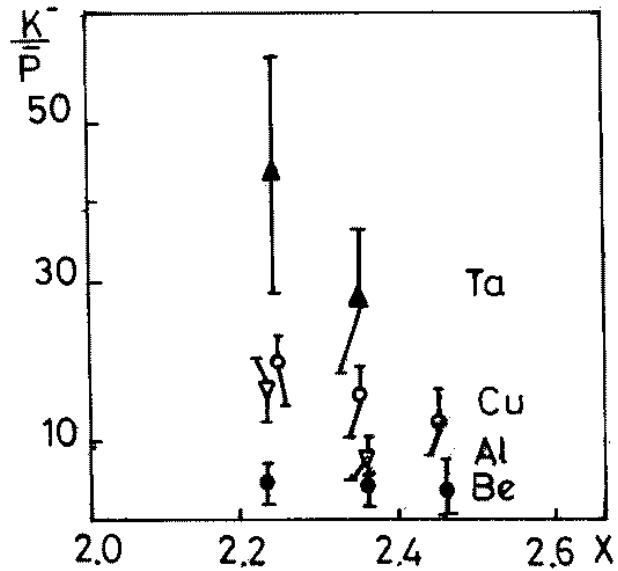
(Boyarinov at al. (89),  $E_{lab}=10$  GeV,  $\theta_{lab}=119^\circ$ )

Nuclei	Be	Al	Ta	Pb
$\Delta_A$ from EMC	0.023	0.036	0.056	0.058
$r_A = (2 - \Delta_A)/\Delta_A$	86	55	36	35



**Low experimental  $r_A$  indicates to "6q"-mechanism of cumulative and EMC-effects.**

$\tilde{P}$  from  $\tilde{q}$ :  $\frac{K^-}{\tilde{p}} \simeq \frac{D_{\tilde{q} \rightarrow K^-}}{D_{\tilde{q} \rightarrow \tilde{p}}} \simeq 10$



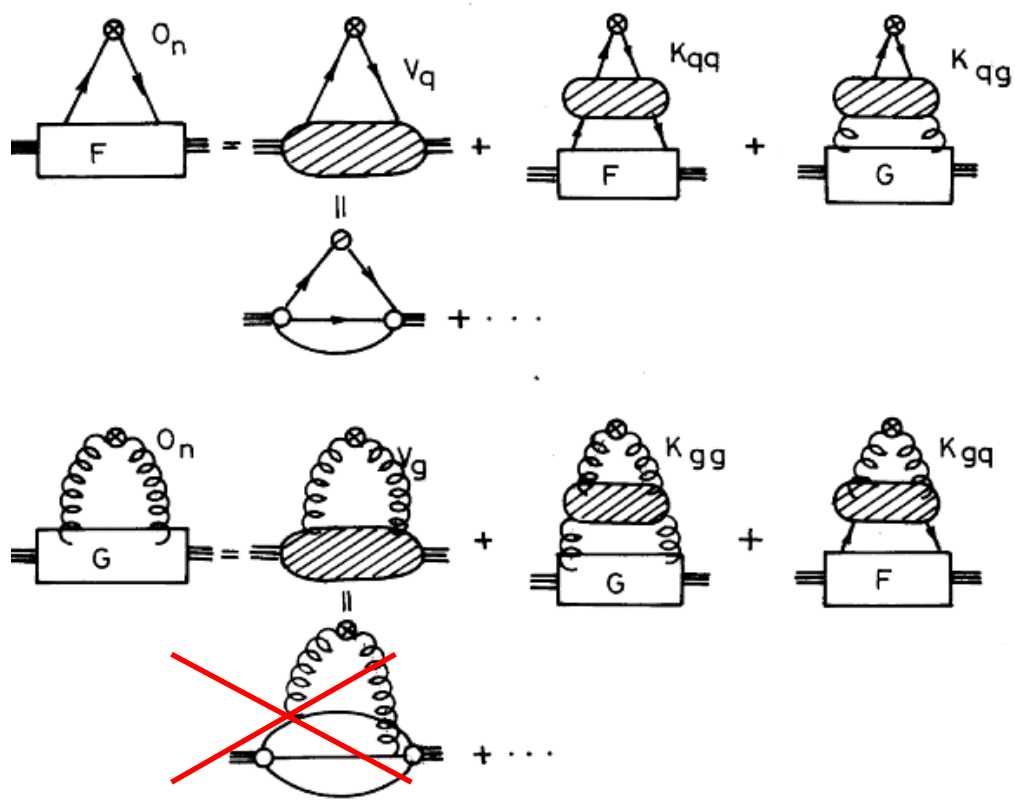
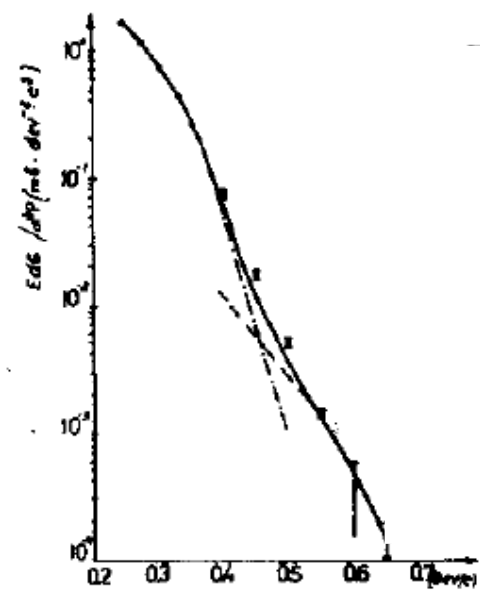
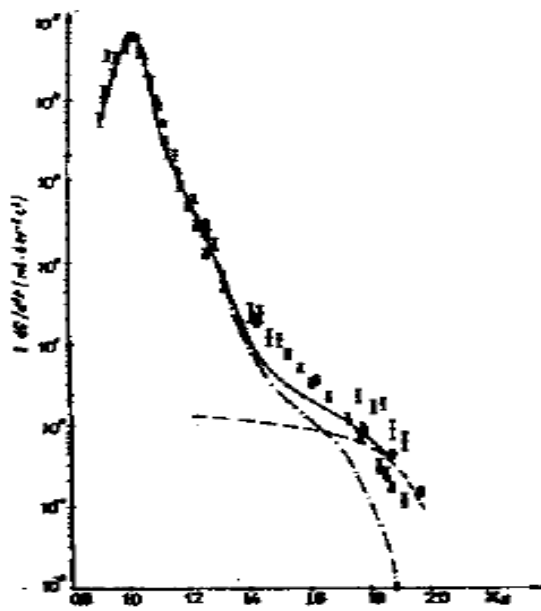
(Boyarinov et al., YaF (91,93),  
 $E_{\text{lab}}=10 \text{ GeV}$ ,  $\theta_{\text{lab}}=119^\circ$  and  
 $\theta_{\text{lab}}=97^\circ$ )

**Again in favor  
of multiquarks!**

## 5. Conclusions

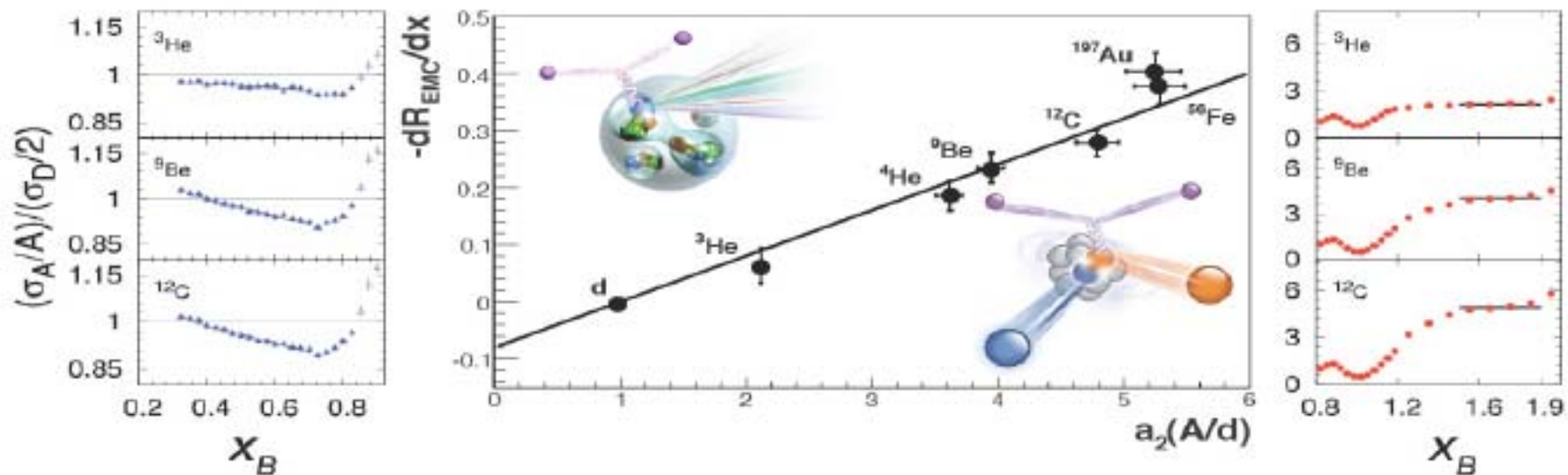
- EMC-effect is repumping of valence quarks to sea quarks momentum,
- Small but hard "collective" sea,
- Evidence for multiquark from cumulative  $K^-$  and  $\tilde{P}$
- Good data for cumulative  $K^-$  and  $\tilde{P}$  for deuterium are necessary of the "collective" sea.
- What are the situation with spin PDFs?

Thanks for attention!





# Some recent work at 6 GeV large $x$ ....



L.B. Weinstein, et al, Phys.Rev.Lett. 106 (2011) 052301